

Latent Class Measurement Model

- LCA model with r observed binary items, u , has a categorical latent variable c with K classes ($c = k; k = 1, 2, \dots, K$). The marginal item probability for item $u_j = 1$,

$$P(u_j = 1) = \sum_{k=1}^K P(c = k)P(u_j = 1 | c = k)$$

LCA: Two sets of parameters

$$P(u_j = 1) = \sum_{k=1}^K \underbrace{P(c = k)}_{\text{STRUCTURAL}} \underbrace{P(u_j = 1 | c = k)}_{\text{MEASUREMENT}}$$

STRUCTURAL: Population proportion of each class.

This is the relative class size:
How big each class is.
E.g., class 1 is 45% of the population

MEASUREMENT: Conditional item probabilities

These are the parameters that define classes. Think of these like the factor loading, as they are how the items relate to the latent variable

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- Assuming **conditional independence**, the joint probability of all the r observed items is

$$P(u_1, u_2, \dots, u_r) = \sum_{k=1}^K P(c = k) P(u_1 | c = k) P(u_2 | c = k) \dots P(u_r | c = k)$$

This is the *default* in Mplus! What does this assumption mean? Is it necessary for the model to be identified? When, if ever, would we relax this assumption?